Analyse d’une enquête sur la sémantique des motifs séquentiels avec négation

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Outline

1. Introduction
2. Syntax and semantics of NSP
3. Design of the survey
4. Gathering survey answers and analysis
5. Conclusions
A **sequence** $s$ is an ordered set of events (or **itemsets**)

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>$s_1$</td>
<td>$\langle a(abc)(ac)d(cf) \rangle$</td>
</tr>
<tr>
<td>$s_2$</td>
<td>$\langle (ab)c(bc)(ae)(ad) \rangle$</td>
</tr>
<tr>
<td>$s_3$</td>
<td>$\langle eg(af)cbc(de) \rangle$</td>
</tr>
</tbody>
</table>
Sequential pattern mining

- A **sequence** $s$ is an ordered set of events (or **itemsets**)
- A **sequential pattern** is a subsequence
  - containment relation: $p \subseteq s$
    - inclusion of itemsets
    - gaps are allowed
  - example:
    - pattern $p = \langle a(bc)d \rangle$
    - embedding: mapping of a pattern on a sequence ($\langle 1, 2, 4 \rangle$, $\langle 1, 3, 5 \rangle$)

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</table>
Sequential pattern mining

- Let $\mathcal{D}$ be a set of sequences,
  - **Frequent pattern mining**: Given a support threshold $\sigma$, find the complete set of sequential patterns with support above $\sigma$
  - the **support** of pattern $p$ in $\mathcal{D}$ is the number of sequences in $\mathcal{D}$ that contain $p$:
    $$supp(p) = |\{s \in \mathcal{D} | p \preceq s\}|$$

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$supp(\langle a(bc)d \rangle) = 2$
Motivation for Negative Sequential Patterns

Positivism of frequent sequential pattern mining
Frequent pattern mining algorithms extract only patterns as subsequences that actually occur!

Problem with frequent sequential pattern mining
- Dataset with hidden frequent patterns
  - sympť₁ → ... → sympťₙ → disease
  - sympť₁ → ... → drug → ... → sympťₙ
  → disease appears only when no drug has been taken
- extracted pattern
  → sympť₁ → ... → sympťₙ
  → not really useful for our problem

What kind of pattern would be interesting?
→ patterns that may highlight the absence of an item (the so-called negative items)
  - sympť₁ → ... → no drug → ... → sympťₙ → disease
Negative sequential patterns in the State of the Art

- Few algorithms extract negative sequential patterns
  - eNSP [CDZ16] and its variants
  - NegGSP [ZZZC09]
  - Gong et al [GLD15]
  - PNSP [HLC08]
  - NegPSpan [GQ20]
- Analysis of the state of the art [BG20]
  - State of the art algorithms do not extract the same patterns
  - There are several semantics for patterns with negation in sequences of itemsets

Our research questions

1. Are there “intuitive” semantics for patterns with negation?
2. Do the “intuitive” semantics correspond to those actually used by one of the algorithms?
3. What recommendations about the use of patterns with negations?
Methodology: survey about the perception of negation in NSP

1. **Identification of alternative interpretations of the negation**
   - We adhere to the analysis of Besnard and Guyet [BG20]
   - \(2^3 = 8\) possible semantics: two alternative perceptions for 3 dimensions

2. **Design of the survey**
   - Should be answered by people without preliminary knowledge about pattern mining
   - Characterization of interviewed
   - Attempt to capture additional bias
   - Anonymity

3. **Collection of answers**
   - Broadcast on national and international mailing lists (in DM and AI)
   - Broadcast to people (personal circles) without preliminary knowledge in data science
   - Attempt to have a broad range of people (not assessed)

4. **Analysis of the survey answers**
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Negative patterns: a syntactic definition [BG20]

We take $\mathcal{I}$ to denote the set of possible items.

**Definition (Negative sequential patterns (NSP))**

A negative pattern $p = \langle p_1 \neg q_1 \ p_2 \neg q_2 \ \ldots \ p_{n-1} \neg q_{n-1} \ p_n \rangle$ is a finite sequence where $p_i \in 2^\mathcal{I} \setminus \emptyset$ for all $i \in [n]$ and $q_i \in 2^\mathcal{I}$ for all $i \in [n-1]$.

**Syntactic limitations on negative sequential patterns**

- an NSP can neither start nor finish with a negative pattern,
- an NSP cannot have two successive negative itemsets,
- an NSP cannot specify positive and negative items in the same position.

We take $\mathcal{N}$ to denote the set of negative sequential patterns.
Semantics of NSP

!!! Spoiler Alert !!!

Do not listen the end of this talk if you want contribute to the survey!

https://tinyurl.com/NegativePatternsSurvey
The **containment relation** between an NSP $p$ and a sequence $s$ defines the **semantics** of NSPs.

Different containment relations lead to different support measures for a pattern, and thus negative sequential pattern mining algorithms does not extract the same pattern set.

8 possible semantics depending on how to consider:

- partial vs total itemset non-inclusion
- soft vs strict embeddings
- weak vs strong occurrences
Partial/total itemset non-inclusion

\[ p_2 = \langle b \neg (cd) a \rangle \]

\[ D_1 = \]

\[ s_1 = \langle b f a \rangle \]
\[ s_2 = \langle b (cf) a \rangle \]
\[ s_3 = \langle b (df) a \rangle \]
\[ s_4 = \langle b (ef) a \rangle \]
\[ s_5 = \langle b (cdef) a \rangle \]

Partial non-inclusion \((\not\subseteq G)\)

\[ s_1 = \langle b f a \rangle \]
\[ s_2 = \langle b (cf) a \rangle \]
\[ s_3 = \langle b (df) a \rangle \]
\[ s_4 = \langle b (ef) a \rangle \]
\[ s_5 = \langle b (cdef) a \rangle \]

Total non-inclusion \((\not\subseteq D)\)

\[ s_1 = \langle b f a \rangle \]
\[ s_2 = \langle b (cf) a \rangle \]
\[ s_3 = \langle b (df) a \rangle \]
\[ s_4 = \langle b (ef) a \rangle \]
\[ s_5 = \langle b (cdef) a \rangle \]
Soft/strict-embeddings

\[ p_3 = \langle a \wedge (bc)d \rangle \]

\[ D_2 = \]

\begin{align*}
  s_1 &= \langle a \ c \ b \ e \ d \rangle \\
  s_2 &= \langle a \ (bc) \ e \ d \rangle \\
  s_3 &= \langle a \ b \ e \ d \rangle \\
  s_4 &= \langle a \ e \ d \rangle \\
\end{align*}

soft-embedding \circ
\[(\forall j \in [e_{i-1} + 1, e_{i+1} - 1], \ q_i \not\in s_j) : \]
\[ s_1 = \langle a \ c \ b \ e \ d \rangle \]
\[ s_2 = \langle a \ (bc) \ e \ d \rangle \]
\[ s_3 = \langle a \ b \ e \ d \rangle \]
\[ s_4 = \langle a \ e \ d \rangle \]

strict-embedding, \bullet
\[(q_i \not\in \bigcup_{j \in [e_{i-1}+1, e_{i+1}-1]} s_j) : \]
\[ s_1 = \langle a \ c \ b \ e \ d \rangle \]
\[ s_2 = \langle a \ (bc) \ e \ d \rangle \]
\[ s_3 = \langle a \ b \ e \ d \rangle \]
\[ s_4 = \langle a \ e \ d \rangle \]
Weak/strong occurrences

\[ p_4 = \langle ab \neg cd \rangle \]

\[ D_3 = \]

\[
\begin{align*}
  s_1 &= \langle a \ b \ e \ d \rangle \\
  s_2 &= \langle a \ b \ c \ d \ e \ b \ d \rangle, \langle a \ b \ c \ d \ e \ b \ d \rangle \\
  s_3 &= \langle a \ e \ d \ b \ e \ d \ d \rangle, \langle a \ e \ d \ b \ e \ d \ d \rangle \\
  s_4 &= \langle a \ e \ d \ b \ c \ e \ d \rangle \\
\end{align*}
\]

weakly-occur, \( \leq \) (there exists):

\[
\begin{align*}
  s_1 &= \langle a \ b \ e \ d \rangle \\
  s_2 &= \langle a \ b \ c \ d \ e \ b \ d \rangle, \langle a \ b \ c \ d \ e \ b \ d \rangle \\
  s_3 &= \langle a \ e \ d \ b \ e \ d \ d \rangle, \langle a \ e \ d \ b \ e \ d \ d \rangle \\
  s_4 &= \langle a \ e \ d \ b \ c \ e \ d \rangle \\
\end{align*}
\]

strongly-occur, \( \sqsubseteq \) (for each positive):

\[
\begin{align*}
  s_1 &= \langle a \ b \ e \ d \rangle \\
  s_2 &= \langle a \ b \ c \ d \ e \ b \ d \rangle, \langle a \ b \ c \ d \ e \ b \ d \rangle \\
  s_3 &= \langle a \ e \ d \ b \ e \ d \ d \rangle, \langle a \ e \ d \ b \ e \ d \ d \rangle \\
  s_4 &= \langle a \ e \ d \ b \ c \ e \ d \rangle \\
\end{align*}
\]
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Overall organisation of the survey

1. Evaluation of the level of knowledge in the domain of pattern mining and/or logic
   - self-assessment of the background knowledge about pattern mining
   - identification of specific skills (computer science, data science, logic)

2. Preliminary check of the understanding of the basics of (positive) sequential patterns
   - One verification question: the user can not access the next questions until s/he correctly answered it

3. 5 questions about the semantics
   - scope of the negation
   - three dimensions of NSP’s semantics: non-inclusion, embeddings, occurrences
   - (one question about the strength of negation vs multiplicity)

- More details about the questions are provided in the article
- Survey: https://tinyurl.com/NegativePatternsSurvey
Example of question: multiple occurrences

According to you, what are the sequences that contain the pattern $p = \langle b \ e f \rangle$?

<table>
<thead>
<tr>
<th>id</th>
<th>Sequence</th>
</tr>
</thead>
<tbody>
<tr>
<td>$o_0$</td>
<td>$\langle b\ a\ f\ d\ b\ d\ f \rangle$</td>
</tr>
<tr>
<td>$o_1$</td>
<td>$\langle b\ a\ f\ d\ e\ b\ d\ f \rangle$</td>
</tr>
<tr>
<td>$o_2$</td>
<td>$\langle d\ b\ e\ c\ a\ d\ f\ b\ d\ e\ f \rangle$</td>
</tr>
<tr>
<td>$o_3$</td>
<td>$\langle b\ a\ f\ b\ a\ e\ f \rangle$</td>
</tr>
</tbody>
</table>

- The user is invited to decide whether a pattern is contained or not in a sequence (*implicit choice of semantics*)
- The examples have been carefully selected to reveal the interpretation of one dimension of the semantics of NSP
Example of question: multiple occurrences

According to you, what are the sequences that contain the pattern $p = \langle b \ b e f \rangle$?

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<tr>
<td>$o_0$</td>
<td>$\langle b \ a f d \ b d f \rangle$</td>
</tr>
<tr>
<td>$o_1$</td>
<td>$\langle b \ a f d e b d f \rangle$</td>
</tr>
<tr>
<td>$o_2$</td>
<td>$\langle d b e c a d f b d e f \rangle$</td>
</tr>
<tr>
<td>$o_3$</td>
<td>$\langle b a f b a e f \rangle$</td>
</tr>
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</table>

- The user is invited to decide whether a pattern is contained or not in a sequence (*implicit choice of semantics*).
- The examples have been carefully selected to reveal the interpretation of one dimension of the semantics of NSP.

- $o_0$, $o_1$ and $o_3 \implies$ weak occurrence
- $o_0 \implies$ strong occurrence
- $o_1$ is a trap ... and is ignored
- other combination of ticks $\implies$ “other” semantics
Example of question: multiple occurrences

According to you, what are the sequences that contain the pattern
\( p = \langle b \, \neg e \, f \rangle \)?

<table>
<thead>
<tr>
<th>id</th>
<th>Sequence</th>
</tr>
</thead>
<tbody>
<tr>
<td>( o_0 )</td>
<td>\langle b , a , f , d , b , d , f \rangle</td>
</tr>
<tr>
<td>( o_1 )</td>
<td>\langle b , a , f , d , e , b , d , f \rangle</td>
</tr>
<tr>
<td>( o_2 )</td>
<td>\langle d , b , e , c , a , d , f , b , d , e , f \rangle</td>
</tr>
<tr>
<td>( o_3 )</td>
<td>\langle b , a , f , b , a , e , f \rangle</td>
</tr>
</tbody>
</table>

- The user is invited to decide whether a pattern is contained or not in a sequence (*implicit choice of semantics*)
- The examples have been carefully selected to reveal the interpretation of one dimension of the semantics of NSP

- \( o_0, o_1 \) and \( o_3 \) \( \Rightarrow \) weak occurrence
- \( o_0 \) \( \Rightarrow \) strong occurrence
- \( o_1 \) is a trap ... and is ignored
- other combination of ticks \( \Rightarrow \) “other” semantics
Two alternative visualisations

According to you, what are the sequences that contain the pattern $p=\langle b \ a\ e\rangle$?

- $\langle f\ f\ b\ d\ c\ e\rangle$
- $\langle f\ b\ d\ f\ c\ e\rangle$
- $\langle d\ f\ b\ d\ c\rangle$
- $\langle d\ b\ d\ e\ a\rangle$
- $\langle f\ c\ b\ e\ d\rangle$

According to you, what are the sequences that contain the pattern $p=\langle \bullet\ \bullet\ \bullet\ \bullet\ \bullet\ \downarrow\rangle$?

- $\langle \bullet\ \bullet\ \bullet\ \bullet\ \bullet\ \downarrow\rangle$
- $\langle \bullet\ \bullet\ \bullet\ \bullet\ \bullet\ \downarrow\rangle$
- $\langle \bullet\ \bullet\ \bullet\ \bullet\ \bullet\ \downarrow\rangle$
- $\langle \bullet\ \bullet\ \bullet\ \bullet\ \bullet\ \downarrow\rangle$
- $\langle \bullet\ \bullet\ \bullet\ \bullet\ \bullet\ \downarrow\rangle$

- Ease the use for uncomfortable people with formal notations
- Prevent from being influenced by an implicit order on events [commented by some surveyed people]

→ we did not collect the information about who used which notation!
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## Gathering answers

### Technical details
- survey in English
- hosted on a personal website (no specific tools used)

### 124 survey answers fully filled
- 54 knowledgeable in data science
- 27 knowledgeable in pattern mining
- 23 knowledgeable in logic
- 40 without specific knowledge in one of these two fields
- 82 researchers

- Survey answers form a large tabular datasets (mainly boolean values)
- Analysis of answers with Formal Concept Analysis
  - Unsupervised identification of groups of people having the same kind of answers
Scope of the negation

**Table:** Result on the question about the scope of negation

<table>
<thead>
<tr>
<th>Scope</th>
<th>Count</th>
<th>Percentage</th>
</tr>
</thead>
<tbody>
<tr>
<td>Conform</td>
<td>101</td>
<td>81.4%</td>
</tr>
<tr>
<td>Conform except $s_4$</td>
<td>9</td>
<td>7.3%</td>
</tr>
<tr>
<td>Alternative</td>
<td>14</td>
<td>11.3%</td>
</tr>
</tbody>
</table>

- $\langle f \ a \ c \ e \ b \rangle$ contains $\langle c \ \neg d \ e \rangle$? Possible different semantic from above

  $\neg e \iff \exists s_i \in s, \ i \in [...], \ s_i \neq e$

  $\rightarrow$ no such situation in the other questions!

- We keep the 110 valid answers in the remaining of the analysis
Occurrence dimension

<table>
<thead>
<tr>
<th>Interpretation</th>
<th>Count</th>
<th>Percentage</th>
</tr>
</thead>
<tbody>
<tr>
<td>Weak relation</td>
<td>75</td>
<td>69.2%</td>
</tr>
<tr>
<td>Strong relation</td>
<td>33</td>
<td>28.2%</td>
</tr>
<tr>
<td>Other</td>
<td>2</td>
<td>3.6%</td>
</tr>
</tbody>
</table>

→ 75 people in concept 3 (weak occurrences: $\alpha_0$, $\alpha_1$ and $\alpha_3$)

→ 33 people in concept 1 (strong occurrences: $\alpha_0$)

Conclusion

Their are two alternative interpretations in the panel: 70% weak / 30% strong occurrences.
Non-inclusion dimension

<table>
<thead>
<tr>
<th>Interpretation</th>
<th>Count</th>
<th>Percentage</th>
</tr>
</thead>
<tbody>
<tr>
<td>Partial non-inclusion</td>
<td>100</td>
<td>90.9%</td>
</tr>
<tr>
<td>Total non-inclusion</td>
<td>3</td>
<td>2.7%</td>
</tr>
<tr>
<td>Other</td>
<td>7</td>
<td>6.4%</td>
</tr>
</tbody>
</table>

Conclusions

→ “Partial non-inclusion” seems to be the most intuitive notion for itemset non-inclusion.
Embedding dimension

<table>
<thead>
<tr>
<th>Interpretation</th>
<th>Count</th>
<th>Percentage</th>
</tr>
</thead>
<tbody>
<tr>
<td>Strict occurrence</td>
<td>97</td>
<td>88.2%</td>
</tr>
<tr>
<td>Soft occurrence</td>
<td>7</td>
<td>6.3%</td>
</tr>
<tr>
<td>Other</td>
<td>6</td>
<td>5.5%</td>
</tr>
</tbody>
</table>

Conclusion

→ the “soft-occurrence” interpretation dominates
Conclusions: there are mainly two semantics that are intuitively used

- Partial non-inclu, soft embedding, strong containment at 23.9%
- Partial non-inclu, soft embedding, weak containment at 69.8%
- The other semantics are marginally represented
Results’ conclusions and recommendations

Conclusions
- There are mainly two semantics that are intuitively used.
- No statistical significant difference between the groups of people (with the characteristics we collected).
- None of the state of the art algorithms fits to the intuition, because of the partial non-inclusion.

Recommendations
1. Use only singletons in the negations. In this case, partial and total non-inclusions are equivalent.
2. Develop an alternative adapted to a partial interpretation of the non-inclusion.
   → Extend preferably NegPSpan regarding its management of multiple occurrences that meets the intuition of a larger number of people.
3. Promote the use of different syntaxes for each semantics.
Discussion (about the methodology)

**Known limits of the methodology**

- **Is the surveyed population representative of potential users of pattern mining algorithms?**
  - not enough questions to describe the population!

- **Non-redundancy of the questions:**
  - strengthen the assignment of an interpretation by multiple questions per dimension

- **‘Small’ number of answers:**
  - it is not so small ... and the results are clear
  - people have conscientiously answered the questions (very poor rate of weird answers)

- **Bias in the presentation of basic notions of sequential patterns**

- **Questionnaire is closely linked to the analysis framework proposed by Besnard and Guyet [BG20], more specifically:**
  - syntactic restrictions
  - 18.5% did not answer as expected to the scope question!
  - Long interviews could complement these results
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Our initial research questions

1. Are there “intuitive” semantics for patterns with negation?
   → There are two dominant ones!

2. Do the “intuitive” semantics correspond to those actually used by one of the algorithms?
   → No, because of the partial non-inclusion

3. What are the recommendations on the use of patterns with negations?
   → extend NegPSpan with partial non-inclusion
   → promote the use of different syntaxes for each semantics

Is pattern mining an “interpretable” data analysis technique?

- pattern mining outputs easy to present results, but
- the existing NSP mining algorithms may leads to data/pattern misinterpretation
- their interpretation requires additional information to prevent from misinterpretation


